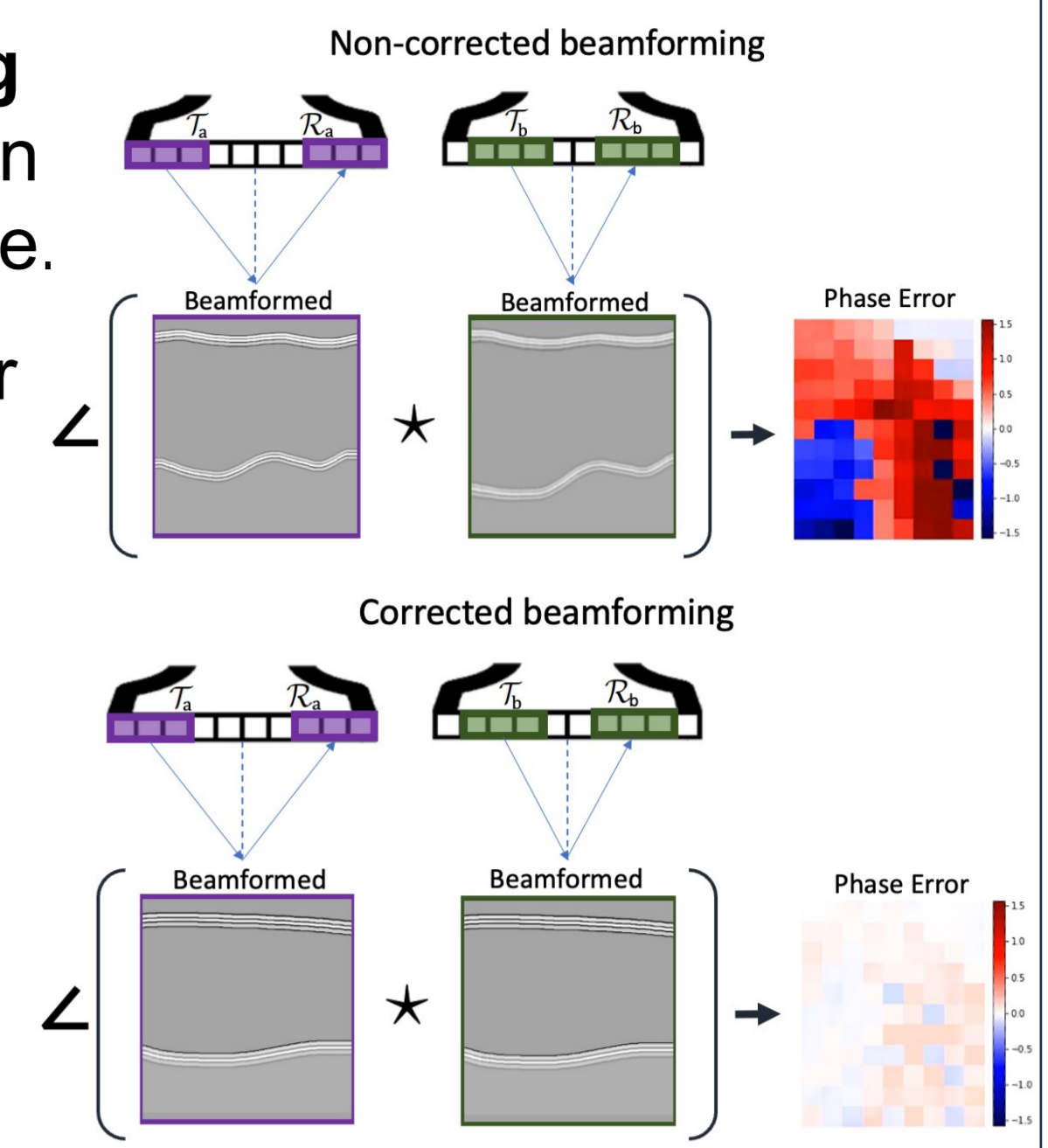


## Motivation

- Most, if not all clinical ultrasound scanners assume a constant sound speed.
- Local sound speed variations in the tissue cause phase aberrations, leading to a loss of image focus, geometric distortions, and reduced diagnostic efficacy.
- Estimated local sound speeds can be used to correct phase aberration and has the potential to be a key diagnostic biomarker.

## Contributions

- We present **differentiable beamforming for ultrasound autofocusing (DBUA)**, a physics-based framework for the rapid quantitative estimation of sound speed and phase aberration correction in heterogeneous tissue.
- We introduce common mid-point phase error from statistical and Fourier optics as a focusing criterion for pulse-echo sound speed estimation.
- DBUA optimizes the common mid-point phase error by differentiating through ultrasound beamforming of sub-apertures and updating sound speed maps via gradient descent.
- DBUA corrects phase aberration in both simulation and *in vivo* settings while simultaneously providing quantitative sound speed maps that can be used for diagnostics (e.g., NAFLD).



## Method

- Beamforming encompasses the process of digitally focusing a received radio-frequency (RF) signal  $u$  recorded on a phased array by sampling at a delayed time  $\tau$  and coherently compounding the sampled signals.

$$u_{ij}(x_k) = u_{ij}(\tau(x_i, x_k) + \tau(x_k, x_j)) \quad u(x_k) = \sum_{i=1}^{N_t} \sum_{j=1}^{N_r} u_{ij}(x_k)$$

- Numerically differentiating beamforming via auto-differentiation is possible with modern numerical libraries, which are often used in deep learning applications.

- We investigate the optimization of a slowness map  $s$  (inverse of sound speed) given an image quality metric.

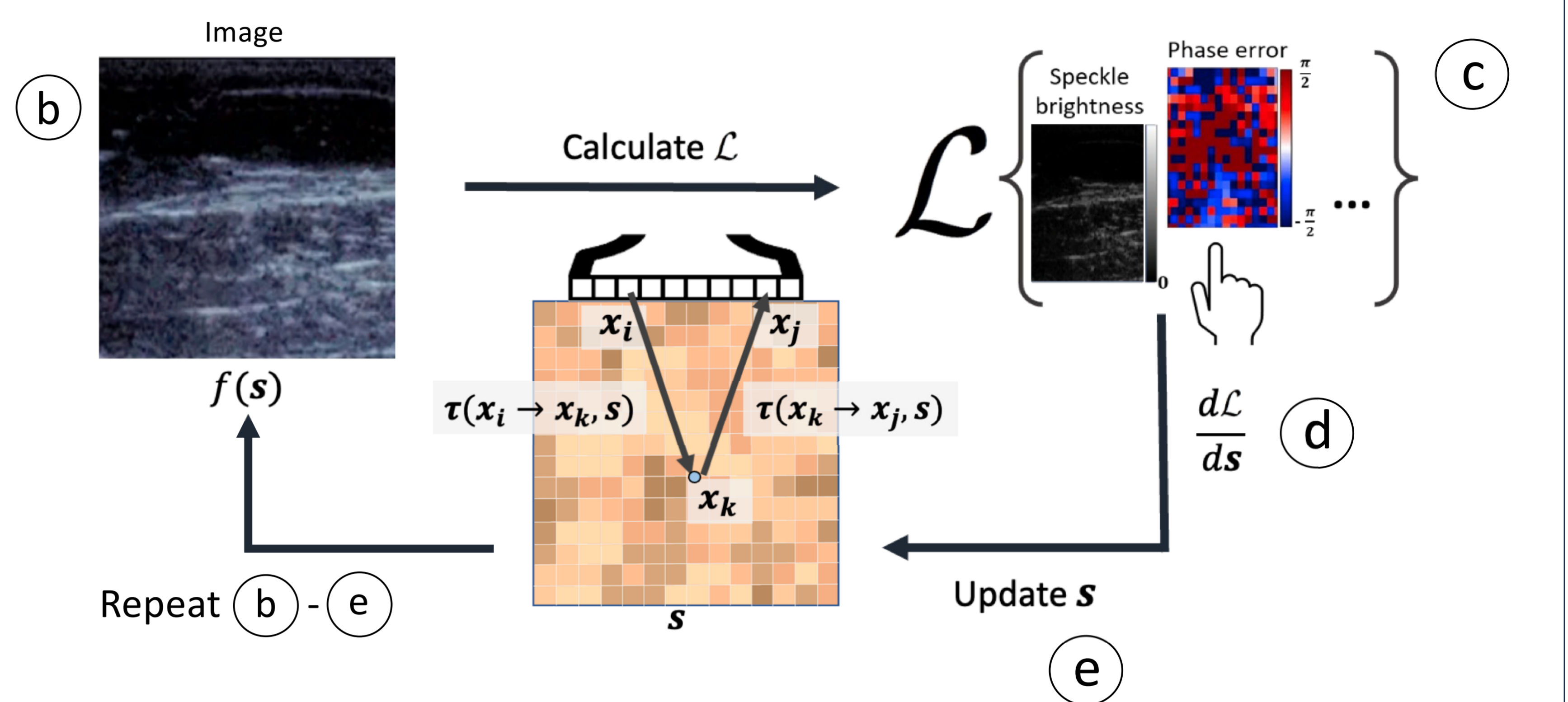
$$s^* = \arg \min_s \mathcal{L}(u(x_k; s)), \quad \Delta s = s - \alpha \frac{\partial}{\partial s} \mathcal{L}(u(x_k; s))$$

- We explore the metrics of **speckle brightness**, **coherence factor**, and **phase error** of common mid-point sub-aperture pairs.

$$SB(s) = \frac{1}{N_k} \sum_k |u(\mathbf{x}_k; s)| = -\mathcal{L}_{SB}(s) \quad CF(s) = \frac{1}{N_k} \sum_{k=1}^{N_k} \frac{|\sum_j \sum_i u_{ij}(\mathbf{x}_k; s)|}{\sum_j |\sum_i u_{ij}(\mathbf{x}_k; s)|} = -\mathcal{L}_{CF}(s)$$

$$\Delta \phi_{ab}(\mathbf{x}_k) = \angle \mathbb{E}[u_a(\mathbf{x}_k; s) u_b^*(\mathbf{x}_k; s)] \quad PE(s) = \frac{1}{N_{(a,b)}} \sum_{(a,b)} |\Delta \phi_{ab}| = \mathcal{L}_{PE}(s)$$

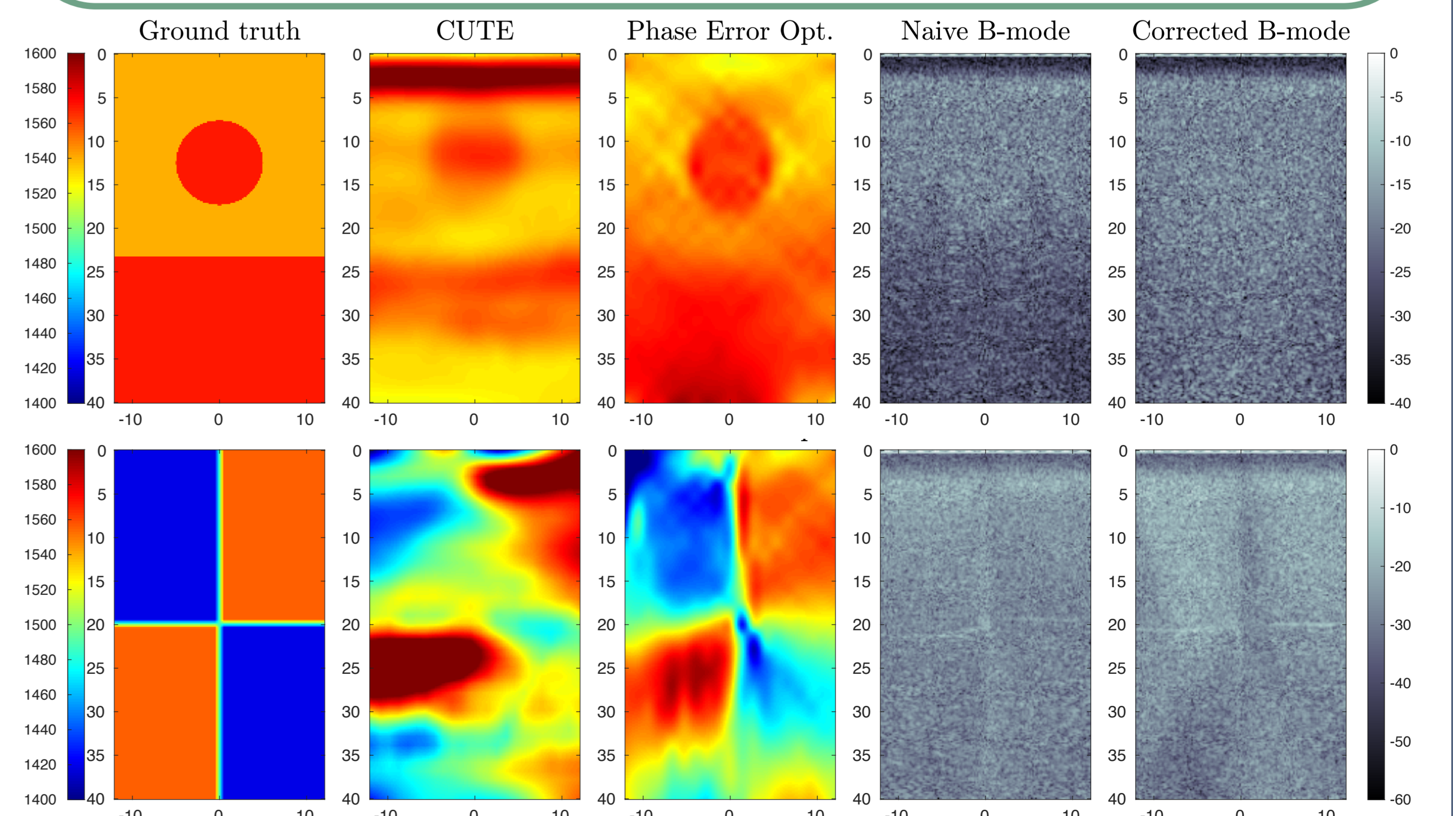
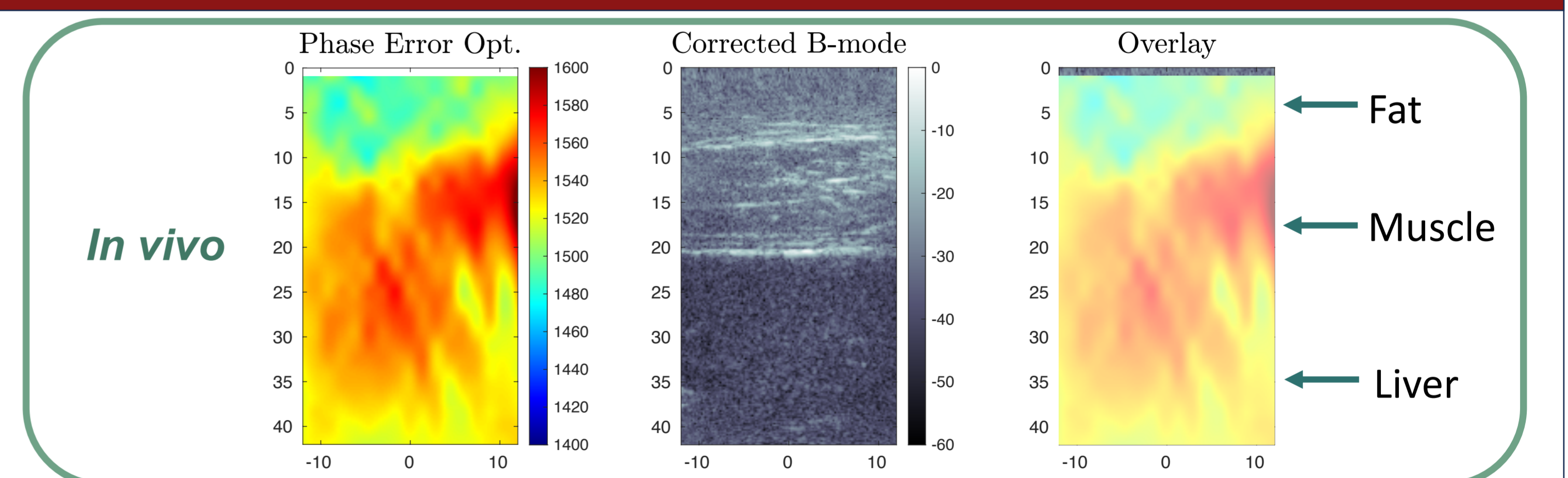
Proposed



- Full-synthetic aperture acquisition
- Delay calculation with straight ray integration and beamforming
- Calculation of objective function
- Backpropagation through beamforming to slowness map
- Update of sound speed map
- Continue from step b.

## Results

- We show that DBUA corrects errors due to aberration while generating quantitative sound speed maps.
- DBUA displays increased resolution when compared to state-of-the-art sound speed reconstruction method CUTE [1].
- DBUA shows promising results on *in vivo* liver data. DBUA resolves fat and abdominal layers.
- DBUA with phase error leads to the lowest quantitative error value in heterogenous phantoms.



Phantom	Description	CUTE (baseline)	Speckle Brightness	Coherence Factor	Phase Error (proposed)
1420	homogenous	21.6±21.4	3.9±3.3	<b>3.2±2.6</b>	4.8±3.5
1465	homogenous	11.7±18.8	4.5±4.9	5.3±4.6	<b>4.5±3.5</b>
1480	homogenous	10.4±18.5	6.1±5.4	<b>4.1±4.2</b>	4.7±3.5
1510	homogenous	10.8±17.0	6.1±7.0	<b>4.4±4.5</b>	4.8±3.6
1540	homogenous	11.8±15.8	7.8±7.5	<b>5.1±4.4</b>	6.1±4.3
1555	homogenous	11.4±15.3	<b>5.7±6.7</b>	5.8±4.7	5.9±4.3
1570	homogenous	11.2±14.8	7.5±7.6	<b>4.9±4.7</b>	6.5±4.7
Quadrant	Fig.3a	65.6±36.3	63.2±52.1	63.4±47.7	<b>35.4±27.9</b>
Two layer	[17]	40.2±34.1	62.5±54.2	33.2±25.8	<b>13.4±14.7</b>
Four layer	[17]	44.1±27.5	50.5±25.0	43.8±23.2	<b>29.0±26.5</b>
Inclusion	[17]	14.3±16.4	8.3±7.5	7.5±5.9	<b>6.1±4.4</b>
Inclusion layer	[17], Fig.3b	19.8±18.1	16.3±14.8	15.0±11.1	<b>7.5±5.0</b>